

# wxMaxima, predavanja

slajd 8, maxima, komandna linija

```
(%i1)      %pi;  
(%o1)       $\pi$   
  
(%i2)      float(%pi);  
(%o2)      3.141592653589793  
  
(%i3)      ev(%pi, numer);  
(%o3)      3.141592653589793  
  
(%i4)      %e;  
(%o4)      %e  
  
(%i5)      float(%e);  
(%o5)      2.718281828459045  
  
(%i6)      float(%i);  
(%o6)      %i  
  
(%i7)      %i^2;  
(%o7)      -1  
  
(%i8)      sqrt(-1);  
(%o8)      %i  
  
(%i9)      sin(%pi/4);  
(%o9)       $\frac{1}{\sqrt{2}}$ 
```

slajd 9, simboli, brojevi, razlomci

```
(%i10)      3/4;  
(%o10)       $\frac{3}{4}$   
  
(%i11)      3.0/4;  
(%o11)      0.75  
  
(%i12)      3/4.;  
(%o12)       $\frac{3}{4}$ 
```

(%i13)  $3/4.0;$

(%o13) 0.75

(%i14)  $\text{float}(3/4);$

(%o14) 0.75

(%i15)  $\text{ev}(3/4, \text{numer});$

(%o15) 0.75

(%i16)  $1/2 - 1/3;$

(%o16)  $\frac{1}{6}$

(%i17)  $\text{float}(%);$

(%o17) 0.16666666666666666

(%i18)  $\sin(2);$

(%o18)  $\sin(2)$

(%i19)  $\sin(2.0);$

(%o19) 0.9092974268256817

(%i20)  $63^3;$

(%o20) 250047

(%i21)  $3^{63};$

(%o21) 1144561273430837494885949696427

(%i22)  $10!;$

(%o22) 3628800

(%i23)  $100!;$

(%o23)

933262154439441526816992388562[98 digits]916864000000000000000000000000

(%i24)  $1000!;$

(%o24)

402387260077093773543702433923[2508 digits]000000000000000000000000000000

slajd 10, problemi sa =, osnovna prepreka primeni

(%i25)  $\text{solve}(2 \cdot x - 8 = 2, x);$

(%o25)  **$[x = 5]$**

(%i26) `solve(x^2-5*x=-6, x);`

(%o26) `[x=3, x=2]`

(%i27) `solve(x^2-2, x);`

(%o27) `[x=-√2, x=√2]`

(%i28) `a;`

(%o28) `a`

(%i29) `a: 4;`

(a) `4`

(%i30) `a;`

(%o30) `4`

(%i31) `a$`

(%i32) `a^3;`

(%o32) `64`

(%i33) `sqrt(a);`

(%o33) `2`

(%i34) `f(x):=x^2;`

(%o34) `f(x):=x2`

(%i35) `f(3);`

(%o35) `9`

(%i36) `f(a);`

(%o36) `16`

(%i37) `f(b);`

(%o37) `b2`

slajd 11, =, % i solve

(%i38) `%;`

(%o38) `b2`

(%i39) `%i245;`

(%o39) `%i245`

```
(%i40) %o245;
```

```
(%o40) %o245
```

```
(%i41) 3·x+2=8;
```

```
(%o41) 3 x + 2 = 8
```

```
(%i42) solve(%, x);
```

```
(%o42) [x = 2]
```

```
(%i43) solve(y^3=27, y);
```

```
(%o43) [y =  $\frac{3^{3/2} \%i - 3}{2}$ , y =  $-\frac{3^{3/2} \%i + 3}{2}$ , y = 3]
```

```
(%i44) solve(f(t)=64, t);
```

```
(%o44) [t = -8, t = 8]
```

slajd 12, undefinisanje

```
(%i45) fundef(f);
```

```
(%o45) f(x) := x2
```

```
(%i46) remfunction(f);
```

```
(%o46) [f]
```

```
(%i47) remfunction(all);
```

```
(%o47) []
```

```
(%i48) values;
```

```
(%o48) [a]
```

```
(%i49) remvalue(a);
```

```
(%o49) [a]
```

```
(%i50) a;
```

```
(%o50) a
```

```
(%i51) a: 2;
```

```
(a) 2
```

```
(%i52) b: 3;
```

```
(b) 3
```

```
(%i53) values;
```

```
(%o53) [a, b]
```

```
(%i54)  remvalue(all);
```

```
(%o54)  [a,b]
```

```
(%i55)  values;
```

```
(%o55)  []
```

slajd 13, kill

```
(%i56)  a: 4;
```

```
(a)      4
```

```
(%i57)  b: 5;
```

```
(b)      5
```

```
(%i58)  f(x):=x^2;
```

```
(%o58)  f(x):=x2
```

```
(%i59)  values;
```

```
(%o59)  [a,b]
```

```
(%i60)  kill(b);
```

```
(%o60)  done
```

```
(%i61)  values;
```

```
(%o61)  [a]
```

```
(%i62)  fundef(f);
```

```
(%o62)  f(x):=x2
```

```
(%i63)  kill(f);
```

```
(%o63)  done
```

```
(%i64)  b: 7;
```

```
(b)      7
```

```
(%i65)  values;
```

```
(%o65)  [a,b]
```

```
(%i66)  kill(all);
```

```
(%o0)   done
```

```
(%i1)   values;
```

```
(%o1)   []
```

slajd 14, jos o funkcijama i ev

(%i2) `f(x):=x^2;`

(%o2) `f(x):=x2`

(%i3) `a: x^2;`

(a) `x2`

(%i4) `f(y);`

(%o4) `y2`

(%i5) `ev(a, x=y);`

(%o5) `y2`

(%i6) `f(4);`

(%o6) `16`

(%i7) `ev(a, x=4);`

(%o7) `16`

slajd 15, fpprec i bfloat

(%i8) `fpprec;`

(%o8) `16`

(%i9) `float(%pi);`

(%o9) `3.141592653589793`

(%i10) `bfloat(%pi);`

(%o10) `3.141592653589793b0`

(%i11) `fpprec: 50;`

(fpprec) `50`

(%i12) `bfloat(%pi);`

(%o12) `3.1415926535897932384626433832795028841971693993751b0`

(%i13) `float(%pi);`

(%o13) `3.141592653589793`

(%i14) `fpprec: 3;`

(fpprec) `3`

```
(%i15) bfloat(%pi);
```

```
(%o15) 3.14b0
```

```
(%i16) float(%pi);
```

```
(%o16) 3.141592653589793
```

slajd 16, fpprintprec

```
(%i17) fpprintprec;
```

```
(%o17) 0
```

```
(%i18) float(%pi);
```

```
(%o18) 3.141592653589793
```

```
(%i19) float(%e);
```

```
(%o19) 2.718281828459045
```

```
(%i20) fpprintprec: 3;
```

```
(fpprintprec) 3
```

```
(%i21) float(%pi);
```

```
(%o21) 3.14
```

```
(%i22) float(%e);
```

```
(%o22) 2.71
```

```
(%i23) fpprintprec: 5;
```

```
(fpprintprec) 5
```

```
(%i24) float(%pi);
```

```
(%o24) 3.1415
```

```
(%i25) float(%e);
```

```
(%o25) 2.7182
```

```
(%i26) fpprintprec: 0;
```

```
(fpprintprec) 0
```

```
(%i27) float(%pi);
```

```
(%o27) 3.141592653589793
```

```
(%i28) float(%e);
```

```
(%o28) 2.718281828459045
```

## slajd 17, expand i factor

(%i29) `expand((x+1)^2);`

(%o29)  $x^2 + 2x + 1$

(%i30) `expand((x+1)·(x-1));`

(%o30)  $x^2 - 1$

(%i31) `expand((x-3)^7);`

(%o31)  $x^7 - 21x^6 + 189x^5 - 945x^4 + 2835x^3 - 5103x^2 + 5103x - 2187$

(%i32) `factor(%);`

(%o32)  $(x - 3)^7$

(%i33) `eq: expand((x-4)·(x-5)·(x-6));`

(eq)  $x^3 - 15x^2 + 74x - 120$

(%i34) `solve(eq, x);`

(%o34)  $[x = 4, x = 5, x = 6]$

(%i35) `factor(eq);`

(%o35)  $(x - 6)(x - 5)(x - 4)$

(%i36) `factor(4·x^5-4·x^4-13·x^3+x^2-17·x+5);`

(%o36)  $(2x - 5)(x^2 + 1)(2x^2 + 3x - 1)$

(%i37) `factor(1001);`

(%o37)  $7 \cdot 11 \cdot 13$

(%i38) `factor(123412341234);`

(%o38)  $2 \cdot 3 \cdot 7 \cdot 13 \cdot 37 \cdot 617 \cdot 9901$

(%i39) `factor(2048);`

(%o39)  $2^{11}$

## slajd 18, parcijalni razlomci, partfrac(expression, variable)

(%i40) `ex: (s^3+4·s^2+6·s+4)/(s^3+3·s^2+3·s+1);`

(ex) 
$$\frac{s^3 + 4s^2 + 6s + 4}{s^3 + 3s^2 + 3s + 1}$$



(%i41) `factor(ex);`

(%o41) 
$$\frac{(s+2)(s^2+2s+2)}{(s+1)^3}$$

(%i42) `partfrac(ex, s);`

(%o42) 
$$\frac{1}{s+1} + \frac{1}{(s+1)^2} + \frac{1}{(s+1)^3} + 1$$

(%i43) `expand(%);`

(%o43) 
$$\frac{1}{s^3+3s^2+3s+1} + \frac{1}{s^2+2s+1} + \frac{1}{s+1} + 1$$

(%i44) `ratsimp(%);`

(%o44) 
$$\frac{s^3+4s^2+6s+4}{s^3+3s^2+3s+1}$$

slajd 19, ratsimp i fullratsimp

(%i45) `kill(all);`

(%o0) `done`

(%i1) `eq: sin(x/(x^2+x))=exp((log(x)+1)^2-log(x)^2);`

(eq) 
$$\sin\left(\frac{x}{x^2+x}\right) = \%e^{(\log(x)+1)^2 - \log(x)^2}$$

(%i2) `ratsimp(eq);`

(%o2) 
$$\sin\left(\frac{1}{x+1}\right) = \%e^{x^2}$$

(%i3) `((x-1)^(3/2)-(x+1)*sqrt(x-1))/sqrt((x-1)*(x+1));`

(%o3) 
$$\frac{(x-1)^{3/2} - \sqrt{x-1}(x+1)}{\sqrt{(x-1)(x+1)}}$$

(%i4) `ratsimp(%);`

(%o4) 
$$-\frac{2\sqrt{x-1}}{\sqrt{x^2-1}}$$

(%i5) `expr: (x^(a/2)+1)^2*(x^(a/2)-1)^2/(x^a-1);`

(expr) 
$$\frac{(x^{a/2}-1)^2(x^{a/2}+1)^2}{x^a-1}$$

(%i6) ratsimp(%);

(%o6) 
$$\frac{x^{2a} - 2x^a + 1}{x^a - 1}$$

(%i7) fullratsimp(%);

(%o7)  $x^a - 1$

slajd 20, trigonometrija

(%i8) cos(%pi/3);

(%o8)  $\frac{1}{2}$

(%i9) sin(%pi/3);

(%o9)  $\frac{\sqrt{3}}{2}$

(%i10) ev(sin(%pi/3), numer);

(%o10) 0.8660254037844386

(%i11) float(sin(%pi/3));

(%o11) 0.8660254037844386

(%i12) csc(45·%pi/180);

(%o12)  $\sqrt{2}$

(%i13) tan(%pi/4);

(%o13) 1

(%i14) tan(%pi/8);

(%o14)  $\tan\left(\frac{\pi}{8}\right)$

(%i15) acos(1/2);

(%o15)  $\frac{\pi}{3}$

(%i16) 180/%pi·asin(sqrt(3)/2);

(%o16) 60

(%i17) acsc(1);

(%o17)  $\frac{\pi}{2}$

## slajd 21, trigonometrija, izrazi

(%i18) `ex: sin(x)^2+cos(x)^2;`

(ex)  $\sin(x)^2 + \cos(x)^2$

(%i19) `trigsimp(ex);`

(%o19) 1

(%i20) `kill(all);`

(%o0) done

(%i1) `ex: sin(a+b);`

(ex)  $\sin(b + a)$

(%i2) `trigexpand(ex);`

(%o2)  $\cos(a) \sin(b) + \sin(a) \cos(b)$

(%i3) `trigrat(%);`

(%o3)  $\sin(b + a)$

(%i4) `ex: sin(x)^2;`

(ex)  $\sin(x)^2$

(%i5) `trigsimp(ex);`

(%o5)  $\sin(x)^2$

(%i6) `trigreduce(ex);`

(%o6) 
$$\frac{1 - \cos(2 x)}{2}$$

(%i7) `trigrat(ex);`

(%o7) 
$$- \frac{\cos(2 x) - 1}{2}$$

## slajd 22, linearni sistemi jednacina 1

(%i8) `3·x+2·y=7;`

(%o8)  $2 y + 3 x = 7$

(%i9) `lhs(%);`

(%o9)  $2 y + 3 x$

```
(%i10)  rhs(%);  
(%o10)  0  
  
(%i11)  rhs(%o253);  
(%o11)  0  
  
(%i12)  e1: 3·x+2·y=7;  
(e1)    2 y + 3 x = 7  
  
(%i13)  lhs(e1);  
(%o13)  2 y + 3 x  
  
(%i14)  rhs(e1);  
(%o14)  7  
  
(%i15)  e2: 5·x-y=3;  
(e2)    5 x - y = 3  
  
(%i16)  linsolve([e1,e2], [x,y]);  
(%o16)  [x = 1, y = 2]  
  
(%i17)  r: %;  
(r)     [x = 1, y = 2]  
  
(%i18)  r[1];  
(%o18)  x = 1  
  
(%i19)  r[2];  
(%o19)  y = 2  
  
(%i20)  rhs(r[1]);  
(%o20)  1  
  
(%i21)  rhs(r[2]);  
(%o21)  2
```

slajd 23, linearni sistemi jednacina 2

```
(%i22)  e1;  
(%o22)  2 y + 3 x = 7  
  
(%i23)  e1: 10·x-2·y=6;  
(e1)    10 x - 2 y = 6
```

(%i24) e2;

(%o24)  $5x - y = 3$

(%i25) linsolve([e1,e2], [x,y]);

**solve: dependent equations eliminated: (2)**

(%o25)  $\left[x = \frac{\%r1 + 3}{5}, y = \%r1\right]$

(%i26) e1: 10·x-2·y=5;

(e1)  $10x - 2y = 5$

(%i27) linsolve([e1,e2], [x,y]);

(%o27) **[]**

slajd 24, eliminacija

(%i28) remvalue(all);

(%o28)  $[ex, bestlength, trylength, e1, e2, r]$

(%i29) a1: x+y+2·t=7;

(a1)  $y + x + 2t = 7$

(%i30) a2: x-y-t=2;

(a2)  $-y + x - t = 2$

(%i31) eliminate([a1,a2], [t]);

(%o31)  $[-y + 3x - 11]$

slajd 25, matrice

(%i32) A: matrix([1,2],[2,1]);

(A)  $\begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$

(%i33) B: invert(A);

(B)  $\begin{bmatrix} -\frac{1}{3} & \frac{2}{3} \\ \frac{2}{3} & -\frac{1}{3} \end{bmatrix}$

(%i34)  $A \cdot B;$

(%o34) 
$$\begin{bmatrix} -\frac{1}{3} & \frac{4}{3} \\ \frac{4}{3} & -\frac{1}{3} \end{bmatrix}$$

(%i35)  $a \cdot B;$

(%o35) 
$$\begin{bmatrix} -\frac{a}{3} & \frac{2a}{3} \\ \frac{2a}{3} & -\frac{a}{3} \end{bmatrix}$$

(%i36)  $A \cdot B;$

(%o36) 
$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

(%i37)  $\text{determinant}(A);$

(%o37)  $-3$

(%i38)  $\text{determinant}(B);$

(%o38)  $-\frac{1}{3}$

(%i39)  $b: \text{matrix}([3],[3]);$

(b) 
$$\begin{bmatrix} 3 \\ 3 \end{bmatrix}$$

(%i40)  $x: B \cdot b;$

(x) 
$$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

(%i41)  $A \cdot x;$

(%o41) 
$$\begin{bmatrix} 3 \\ 3 \end{bmatrix}$$

(%i42)  $A \cdot x - b;$

(%o42) 
$$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

(%i43)  $\text{kill}(\text{all});$

(%o0)  $\text{done}$

## slajd 26, Kronecker-Capelli

(%i1) **A:** matrix([5,-1,3],[10,-2,6]);

(A) 
$$\begin{bmatrix} 5 & -1 & 3 \\ 10 & -2 & 6 \end{bmatrix}$$

(%i2) **echelon(A);**

(%o2) 
$$\begin{bmatrix} 1 & -\frac{1}{5} & \frac{3}{5} \\ 0 & 0 & 0 \end{bmatrix}$$

(%i3) **A[2][3]: 5;**

(%o3) 5

(%i4) **A;**

(%o4) 
$$\begin{bmatrix} 5 & -1 & 3 \\ 10 & -2 & 5 \end{bmatrix}$$

(%i5) **echelon(A);**

(%o5) 
$$\begin{bmatrix} 1 & -\frac{1}{5} & \frac{3}{5} \\ 0 & 0 & 1 \end{bmatrix}$$

## slajd 27, nelinearni sistemi

(%i6) **remvalue(all);**

(%o6) **[A]**

(%i7) **a1: x^2+y^2=41;**

(a1) 
$$y^2 + x^2 = 41$$

(%i8) **a2: y=x+1;**

(a2) 
$$y = x + 1$$

(%i9) **algsys([a1,a2],[x,y]);**

(%o9) **[[x=4,y=5],[x=-5,y=-4]]**

(%i10) **t: solve(a1, y);**

(t) 
$$[y = -\sqrt{41 - x^2}, y = \sqrt{41 - x^2}]$$

(%i11) **y1: rhs(t[1]);**

(y1) 
$$-\sqrt{41 - x^2}$$

```
(%i12)  y2: rhs(t[2]);
```

```
(y2)     $\sqrt{41 - x^2}$ 
```

```
(%i13)  solve(a2, y);
```

```
(%o13)  [y = x + 1]
```

```
(%i14)  y3: rhs(solve(a2, y)[1]);
```

```
(y3)    x + 1
```

slajd 28, plotovanje

```
(%i15)  plot2d([y1,y2,y3],[x,-10,10],[y,-15,15]);
```

**plot2d: expression evaluates to non-numeric value somewhere in plotting range**

**plot2d: expression evaluates to non-numeric value somewhere in plotting range**

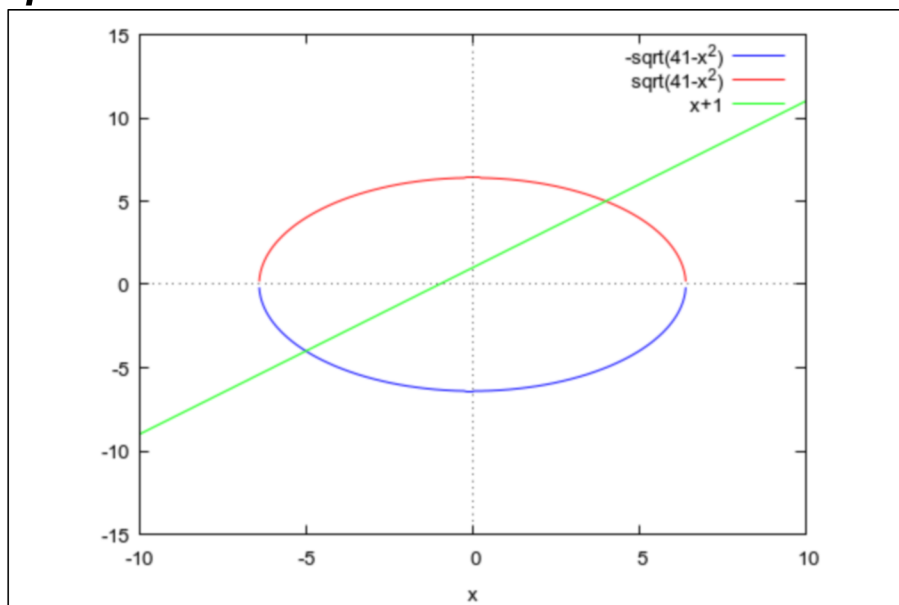
```
(%o15)  [/tmp/maxout11052.gnuplot_pipes]
```

```
(%i16)  wxplot2d([y1,y2,y3],[x,-10,10],[y,-15,15]);
```

**plot2d: expression evaluates to non-numeric value somewhere in plotting range**

**plot2d: expression evaluates to non-numeric value somewhere in plotting range**

```
(%t16)
```



```
(%o16)
```

slajd 29, limesi

```
(%i17)  limit((1+1/x)^(2*x), x, inf);
```

```
(%o17)  %e2
```

```
(%i18)  float(%);
```

```
(%o18)  7.38905609893065
```



(%i19)  $(x-2)/(x^2-4);$

(%o19)  $\frac{x-2}{x^2-4}$

(%i20)  $\text{limit}(\%, x, 2);$

(%o20)  $\frac{1}{4}$

(%i21)  $f(x):=\text{atan}(x);$

(%o21)  $f(x):=\text{atan}(x)$

(%i22)  $\text{limit}(f(x), x, \text{inf});$

(%o22)  $\frac{\pi}{2}$

(%i23)  $\text{limit}(f(x), x, \text{minf});$

(%o23)  $-\frac{\pi}{2}$

(%i24)  $\text{limit}(x^3, x, \text{inf});$

(%o24)  $\infty$

(%i25)  $\text{limit}(x^3, x, \text{minf});$

(%o25)  $-\infty$

(%i26)  $\text{limit}(\sin(3 \cdot x)/x, x, 0);$

(%o26)  $3$

(%i27)  $\text{limit}(\sin(3 \cdot x)/x, x, \text{inf});$

(%o27)  $0$

(%i28)  $\text{limit}(\sin(3 \cdot x)/x, x, \text{minf});$

(%o28)  $0$

slajd 30, kombinacije . . .

(%i29)  $f(x):=x^3 \cdot \tan(x);$

(%o29)  $f(x):=x^3 \tan(x)$

(%i30)  $\text{rd: } (f(x+h)-f(x))/h;$

(rd) 
$$\frac{(x+h)^3 \tan(x+h) - x^3 \tan(x)}{h}$$

(%i31) `limit(rd, h, 0);`

(%o31)  $3x^2 \tan(x) + \frac{x^3}{\cos(x)^2}$

(%i32) `trigsimp(%);`

(%o32)  $\frac{3x^2 \cos(x) \sin(x) + x^3}{\cos(x)^2}$

(%i33) `trigrat(%);`

(%o33)  $\frac{3x^2 \sin(2x) + 2x^3}{\cos(2x) + 1}$

slajd 31, 0, 0- i 0+

(%i34) `limit(1/x, x, 0);`

(%o34) *infinity*

(%i35) `limit(1/x, x, 0, plus);`

(%o35)  $\infty$

(%i36) `limit(1/x, x, 0, minus);`

(%o36)  $-\infty$

slajd 32, izvodi

(%i37) `remvalue(all);`

(%o37) **`[a1, a2, t, y1, y2, y3, rd, bestlength, trylength]`**

(%i38) `diff(x^2, x);`

(%o38)  $2x$

(%i39) `diff(sin(x), x);`

(%o39)  $\cos(x)$

(%i40) `diff(sin(x), x, 2);`

(%o40)  $-\sin(x)$

(%i41) `diff(sin(x), x, 3);`

(%o41)  $-\cos(x)$

(%i42) `diff(sin(x), x, 4);`

(%o42)  $\sin(x)$

```
(%i43) diff(sin(x·y), x);
```

```
(%o43) y cos(x y)
```

```
(%i44) diff(sin(w·t), t);
```

```
(%o44) w cos(t w)
```

slajd 33, razvoj u red

```
(%i45) taylor(sin(x), x, 0, 5);
```

```
(%o45)/T/  $x - \frac{x^3}{6} + \frac{x^5}{120} + \dots$ 
```

```
(%i46) taylor(cos(x), x, 0, 7);
```

```
(%o46)/T/  $1 - \frac{x^2}{2} + \frac{x^4}{24} - \frac{x^6}{720} + \dots$ 
```

```
(%i47) f(x):=%e^x-cos(x);
```

```
(%o47) f(x):=%e^x-cos(x)
```

```
(%i48) taylor(f(x), x, 0, 7);
```

```
(%o48)/T/  $x + x^2 + \frac{x^3}{6} + \frac{x^5}{120} + \frac{x^6}{360} + \frac{x^7}{5040} + \dots$ 
```

slajd 34, integrali

```
(%i49) integrate(x^2, x);
```

```
(%o49)  $\frac{x^3}{3}$ 
```

```
(%i50) integrate(sin(x), x);
```

```
(%o50)  $-\cos(x)$ 
```

```
(%i51) integrate(x^2, x, 1, 2);
```

```
(%o51)  $\frac{7}{3}$ 
```

```
(%i52) integrate(sin(x), x, 0, %pi);
```

```
(%o52) 2
```

```
(%i53) integrate(1/(1+x^2), x, 0, 1);
```

```
(%o53)  $\frac{\pi}{4}$ 
```

## slajd 35, operator '

```
(%i54) kill(all);
```

```
(%o0) done
```

```
(%i1) a: 4;
```

```
(a) 4
```

```
(%i2) a;
```

```
(%o2) 4
```

```
(%i3) 'a;
```

```
(%o3) a
```

```
(%i4) 'diff(x^2, x);
```

```
(%o4)  $\frac{d}{dx} x^2$ 
```

```
(%i5) 'integrate(x^2, x);
```

```
(%o5)  $\int x^2 dx$ 
```

```
(%i6) ev(%, integrate);
```

```
(%o6)  $\frac{x^3}{3}$ 
```

```
(%i7) 'integrate(x^2, x, 0, 1);
```

```
(%o7)  $\int_0^1 x^2 dx$ 
```

```
(%i8) ev(%, integrate);
```

```
(%o8)  $\frac{1}{3}$ 
```

## slajd 36, uvod u diferencijalne jednacine

(%i9) eq1: 'diff(y, t, 2) + 4 · y = 0;

(eq1)  $\frac{d^2}{dt^2} y + 4 y = 0$

(%i10) ode2(eq1, y, t);

(%o10)  $y = \%k1 \sin(2 t) + \%k2 \cos(2 t)$

(%i11) eq2: 'diff(y, t, 2) - 4 · y = 0;

(eq2)  $\frac{d^2}{dt^2} y - 4 y = 0$

(%i12) ode2(eq2, y, t);

(%o12)  $y = \%k1 e^{2 t} + \%k2 e^{-2 t}$

(%i13) eq3: 'diff(y, t, 2) - 2 · 'diff(y, t) + y = 0;

(eq3)  $\frac{d^2}{dt^2} y - 2 \left( \frac{d}{dt} y \right) + y = 0$

(%i14) ode2(eq3, y, t);

(%o14)  $y = (\%k2 t + \%k1) e^t$

(%i15) eq4: 'diff(y,t,2)+2·'diff(y,t)+4·y=8·sin(4·t);

(eq4)  $\frac{d^2}{dt^2} y + 2 \left( \frac{d}{dt} y \right) + 4 y = 8 \sin(4 t)$

(%i16) ode2(eq4, y, t);

(%o16)  $y = \%e^{-t} (\%k1 \sin(\sqrt{3} t) + \%k2 \cos(\sqrt{3} t)) - \frac{6 \sin(4 t) + 4 \cos(4 t)}{13}$

13

slajd 37, provera resenja, substitute

(%i17) eq: 'diff(y, t, 2) + y = 0;

(eq)  $\frac{d^2}{dt^2} y + y = 0$

(%i18) s: ode2(eq, y, t);

(s)  $y = \%k1 \sin(t) + \%k2 \cos(t)$

(%i19) s: rhs(s);

(s)  $\%k1 \sin(t) + \%k2 \cos(t)$

```
(%i20) p: subst(s, y, eq);
```

```
(p) 
$$\frac{d^2}{dt^2} (\%k1 \sin(t) + \%k2 \cos(t)) + \%k1 \sin(t) + \%k2 \cos(t)$$

= 0
```

```
(%i21) ev(p, diff);
```

```
(%o21) 0 = 0
```

```
(%i22) is(%);
```

```
(%o22) true
```

slajd 38, scripting

```
(%i23) batch("dj.mac");
```

**read and interpret file: #p/home/peja/Desktop/skloni/PSAE-sve/PSAE-sources-20**

```
(%i24) eq1:'diff(y,t,2)+4*y = 0
```

```
(%o24) 
$$\frac{d^2}{dt^2} y + 4 y = 0$$

```

```
(%i25) ode2(eq1,y,t)
```

```
(%o25) y = \%k1 sin(2 t) + \%k2 cos(2 t)
```

```
(%i26) eq2:'diff(y,t,2)-4*y = 0
```

```
(%o26) 
$$\frac{d^2}{dt^2} y - 4 y = 0$$

```

```
(%i27) ode2(eq2,y,t)
```

```
(%o27) y = \%k1 %e2 t + \%k2 %e-2 t
```

```
(%i28) eq3:'diff(y,t,2)-2*'diff(y,t)+y = 0
```

```
(%o28) 
$$\frac{d^2}{dt^2} y - 2 \left( \frac{d}{dt} y \right) + y = 0$$

```

```
(%i29) ode2(eq3,y,t)
```

```
(%o29) y = (%k2 t + \%k1) %et
```

```
(%i30) eq4:'diff(y,t,2)+2*'diff(y,t)+4*y = 8*sin(4*t)
```

```
(%o30) 
$$\frac{d^2}{dt^2} y + 2 \left( \frac{d}{dt} y \right) + 4 y = 8 \sin(4 t)$$

```

```
(%i31) ode2(eq4,y,t)
```

```
(%o31) y = %e-t (%k1 sin(√3 t) + \%k2 cos(√3 t)) -
```

```
6 sin(4 t) + 4 cos(4 t)
```

13

```
(%o31) dj.mac
```

slajd 39, Laplasova transformacija

```
(%i32) kill(all);
```

```
(%o0) done
```

(%i1) `laplace(1, t, s);`

(%o1)  $\frac{1}{s}$

(%i2) `laplace(sin(w·t), t, s);`

(%o2)  $\frac{w}{w^2 + s^2}$

(%i3) `laplace(cos(w·t), t, s);`

(%o3)  $\frac{s}{w^2 + s^2}$

(%i4) `laplace(exp(a·t), t, s);`

(%o4)  $\frac{1}{s - a}$

(%i5) `laplace(exp(a·t)·sin(w·t), t, s);`

(%o5)  $\frac{w}{w^2 + s^2 - 2 a s + a^2}$

(%i6) `laplace(exp(a·t)·cos(w·t), t, s);`

(%o6)  $\frac{s - a}{w^2 + s^2 - 2 a s + a^2}$

(%i7) `laplace(exp(t-T), t, s);`

(%o7)  $\frac{\%e^{-T}}{s - 1}$

slajd 40, inverzna Laplasova transformacija

(%i8) `ilt(1/(s+2), s, t);`

(%o8)  $\%e^{-2 t}$

(%i9) `ilt(2/(s^2+4), s, t);`

(%o9)  $\sin(2 t)$

(%i10) `ilt((s^2+3·s+3)/(s^3+3·s^2+3·s+1), s, t);`

(%o10)  $\frac{t^2 \%e^{-t}}{2} + t \%e^{-t} + \%e^{-t}$

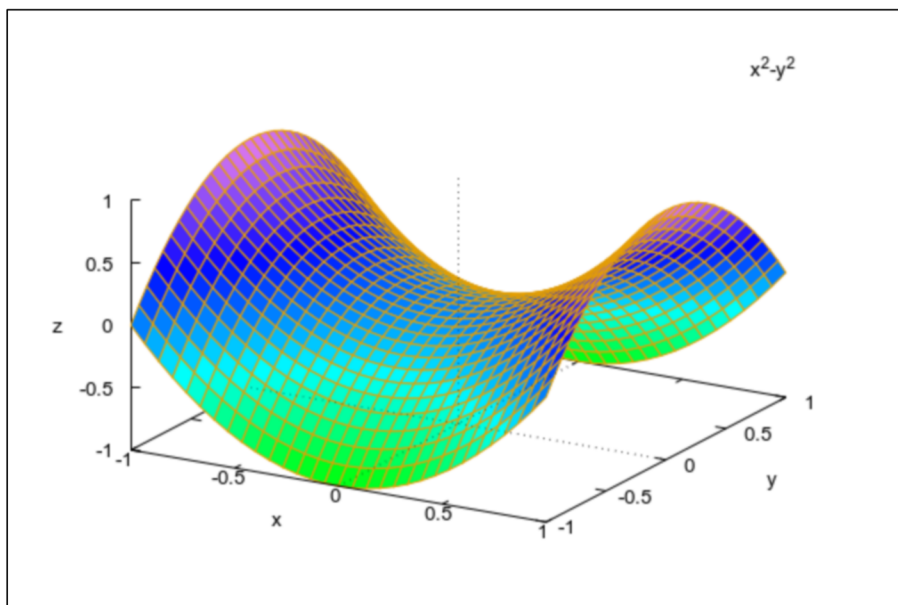
slajd 40, wxMaxima

```
(%i11) plot3d(x^2-y^2, [x,-1,1], [y,-1,1]);
```

```
(%o11) [/tmp/maxout11052.gnuplot_pipes]
```

```
(%i12) wxplot3d(x^2-y^2, [x,-1,1], [y,-1,1]);
```

```
(%t12)
```



```
(%o12)
```